

Exple $f(x) = \frac{1}{x^2+3}$

$$u = 1 \quad v = x^2 + 3$$

$$u' = 0 \quad v' = 2x$$

$$\left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2}$$

$$f'(x) = \frac{0 \cdot (x^2+3) - 1 \cdot 2x}{(x^2+3)^2} = -\frac{2x}{(x^2+3)^2}$$

$$\Rightarrow \boxed{\left(\frac{1}{v}\right)' = -\frac{v'}{v^2}}$$

Ex 2.7.18

g) $f(x) = \frac{5}{(2x^2-1)}$

$$v = 2x^2 - 1$$

$$v' = 4x$$

$$f'(x) = 5 \left(\frac{1}{2x^2-1}\right)' = 5 \cdot \left(-\frac{4x}{(2x^2-1)^2}\right) = -\frac{20x}{(2x^2-1)^2}$$

Règles de dérivation (suite et fin)

$$5. \quad (u \circ v(x))' = (u(v(x)))' = \underline{u'(v(x))} \cdot \underbrace{v'(x)}_{\substack{\uparrow \\ \text{dérivée interne}}}$$

en particulier :

$$5.1 \quad ((u)^n)' = n \cdot u^{n-1} \cdot u'$$

$$\text{exemple : } (x^3 + 3x + 1)^5 = 5(x^3 + 3x + 1)^4 (3x^2 + 3)$$

$$u = x^3 + 3x + 1$$

$$u' = 3x^2 + 3$$

$$5.2 \quad (\sqrt{u})' = \frac{1}{2\sqrt{u}} \cdot u' = \frac{u'}{2\sqrt{u}}$$

$$\text{exple : } (\sqrt{x^2 + 2x})' = \frac{2x+2}{2\sqrt{x^2+2x}} = \frac{\cancel{2}(x+1)}{\cancel{2}\sqrt{x^2+2x}} = \frac{x+1}{\sqrt{x^2+2x}}$$

$$u = x^2 + 2x$$

$$u' = 2x + 2$$

Exemples: a) $f(x) = \frac{(x-1)^3}{x+2}$

$$u = (x-1)^3 \quad v = x+2$$

$$u' = 3(x-1)^2 \cdot 1 \quad v' = 1$$

$$f'(x) = \frac{3(x-1)^2(x+2) - (x-1)^3}{(x+2)^2}$$

$$= \frac{(x-1)^2 [3(x+2) - (x-1)]}{(x+2)^2}$$

$$= \frac{(x-1)^2 (3x+6-x+1)}{(x+2)^2} = \frac{(x-1)^2 (2x+7)}{(x+2)^2}$$

$$f'(x) = \frac{u'v - uv'}{v^2}$$

b) $f(x) = \frac{(2x-5)^2}{x^3}$

$$u = (2x-5)^2 \quad v = x^3$$

$$u' = 2(2x-5) \cdot 2 \quad v' = 3x^2$$

$$= 4(2x-5)$$

$$f'(x) = \frac{4x^3(2x-5) - 3x^2(2x-5)^2}{x^6} = \frac{\cancel{x^2}(2x-5)[4x - 3(2x-5)]}{x^{\cancel{6}4}}$$

$$= \frac{(2x-5)(4x-6x+15)}{x^4} = \frac{(2x-5)(-2x+15)}{x^4}$$